



Prototype HR2 Heat Release
Apparatus Under
Development

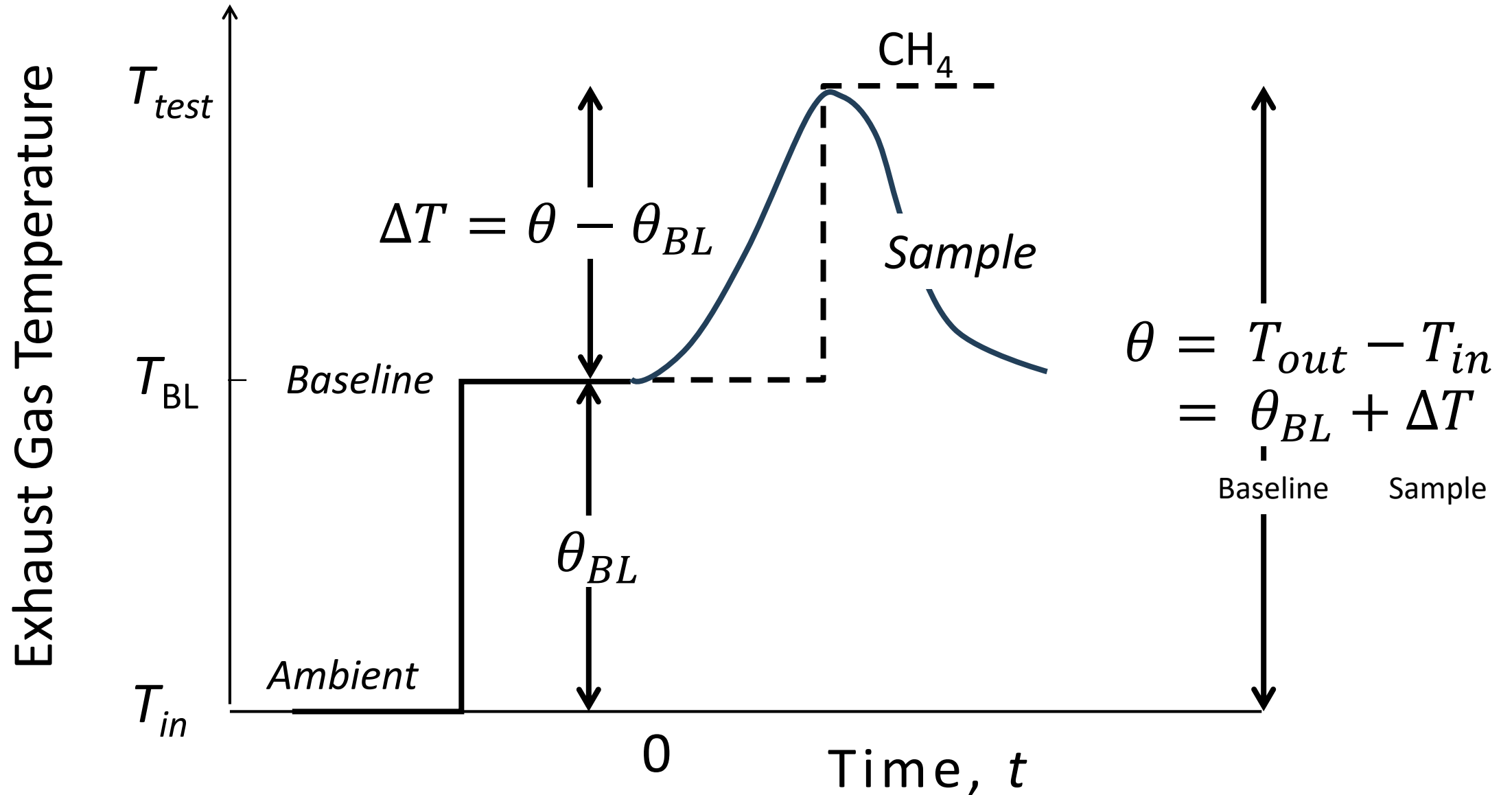
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HR2 Heat Transfer Model



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Temperature Histories in HR2



HR2 Standard Operation

According to the Fire Test Handbook

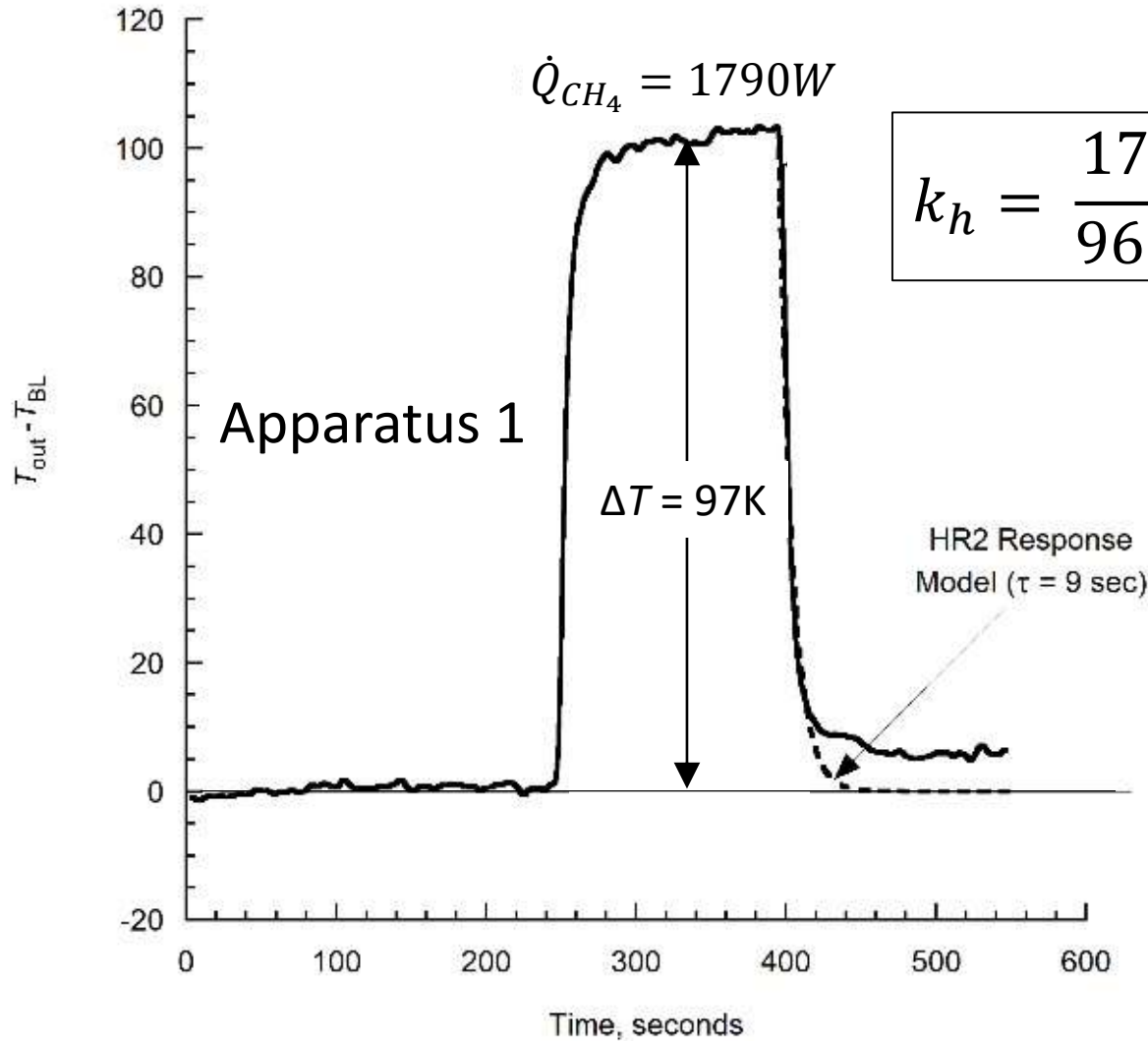
**Calibration
Factor (Static)**

$$k_h = \frac{\dot{Q}_{CH_4}}{\Delta T_{CH_4}} = \frac{(H_c \rho \dot{V})_{CH_4}}{\Delta T_{CH_4}} \approx 20 \frac{W}{K}$$

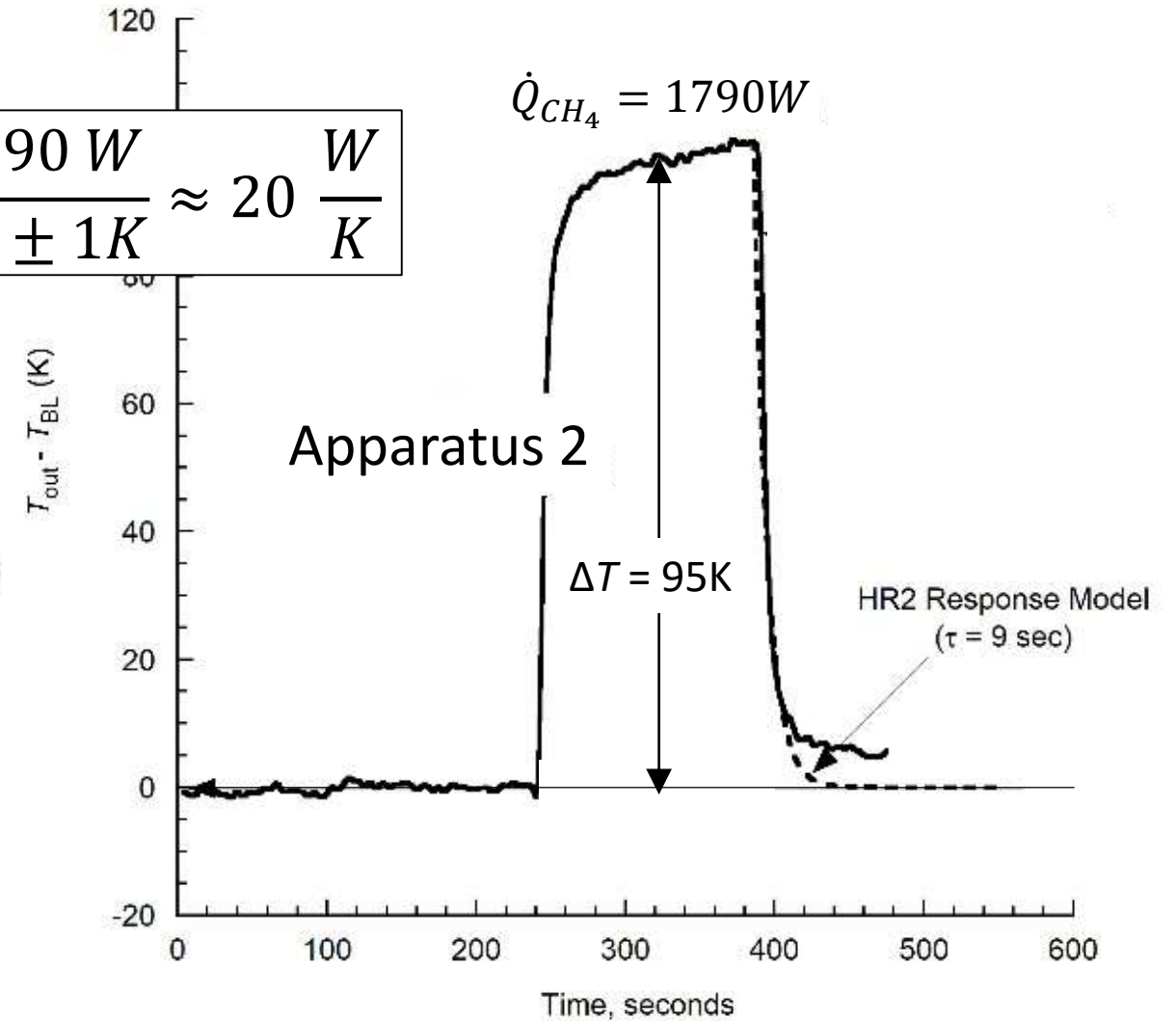
**Heat Release Rate
(Static Calibration)**

$$\text{HRR} \left(\frac{W}{m^2} \right) = \frac{\text{Combustion Rate}}{\text{Sample Area}} = \frac{\dot{Q}(t)}{A} = k_h \frac{\Delta T(t)}{A}$$

Methane Calibration



$$k_h = \frac{1790 W}{96 \pm 1K} \approx 20 \frac{W}{K}$$



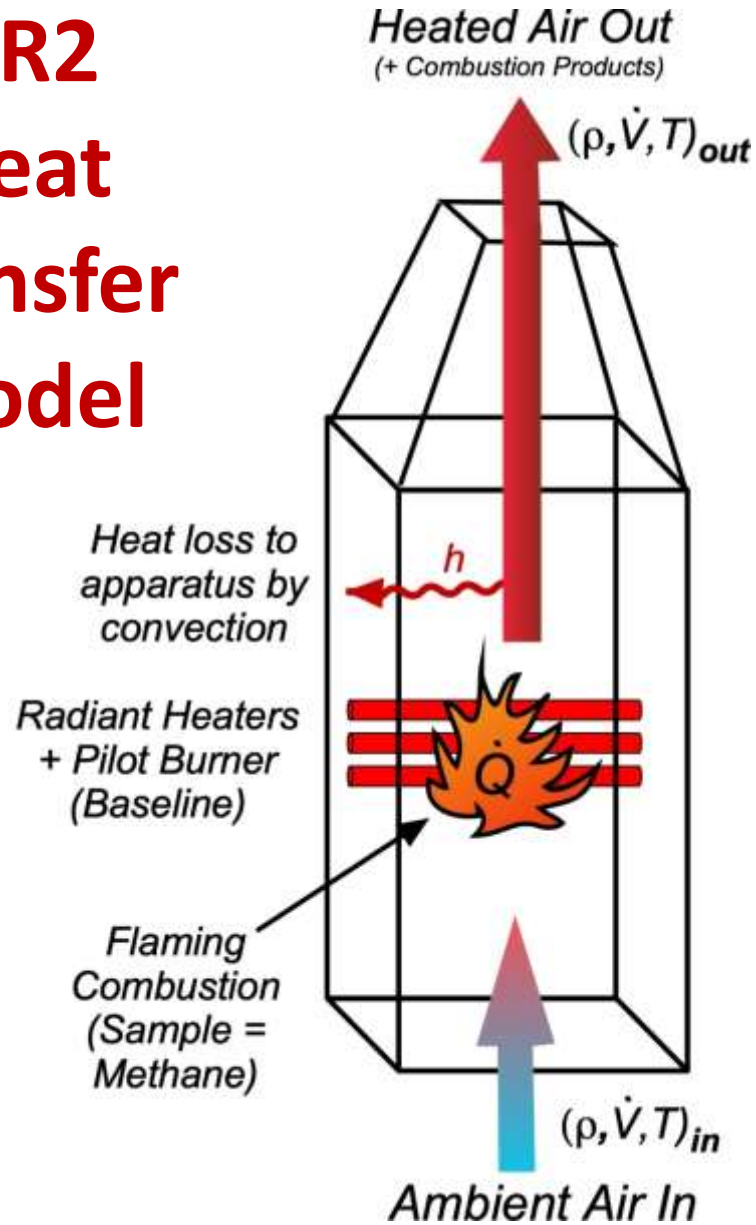
Problem Statement

The standard procedure with static methane calibration doesn't tell us anything about how the dynamics of the HR2 affect the HRR results

Potential Solution

Develop and validate a heat transfer model for the HR2

HR2 Heat Transfer Model



Mass Balance

$$(\rho \dot{V})_{out} = (\rho \dot{V})_{in}$$

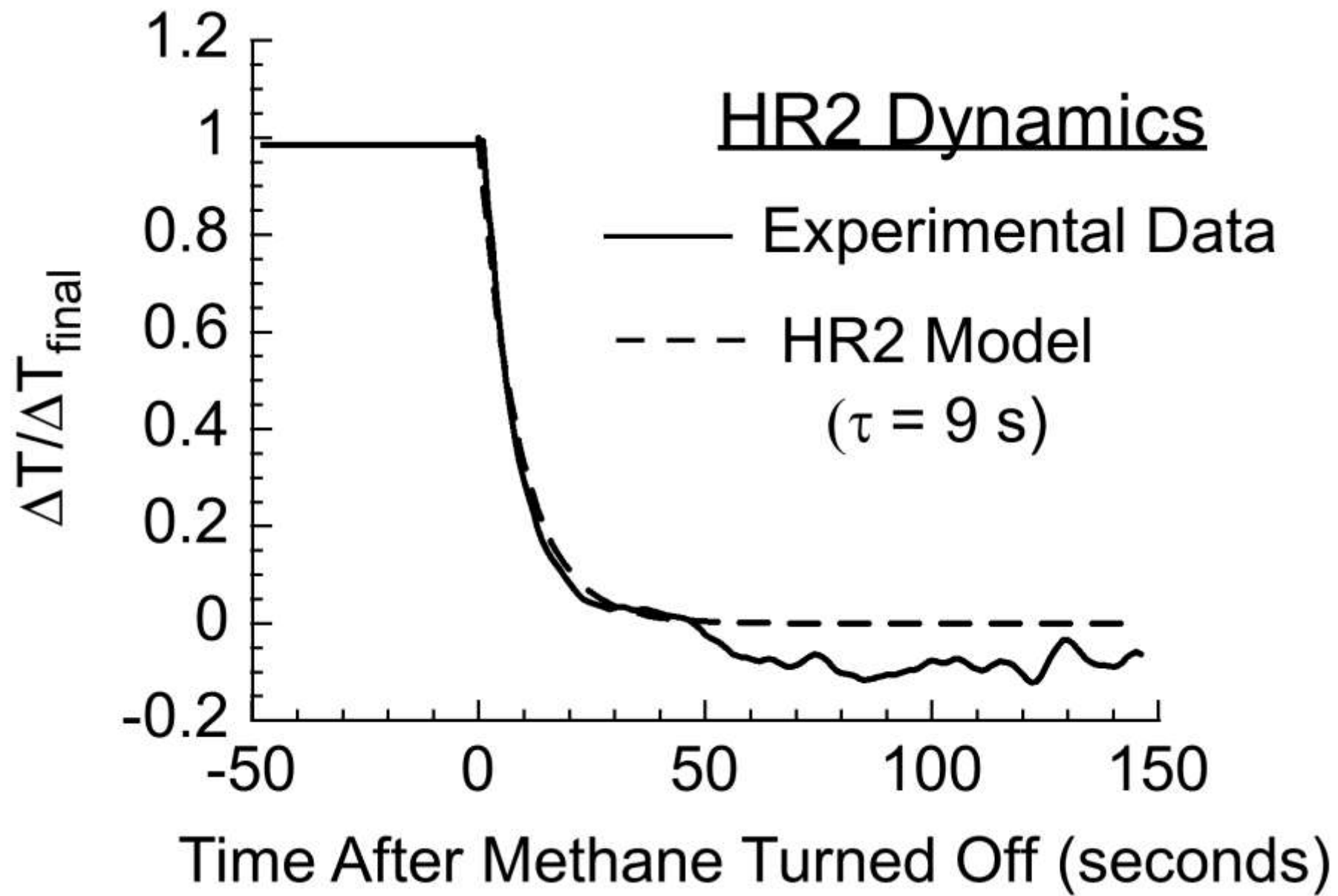
Energy Balance ($\theta = T_{out} - T_{in}$)

$$\frac{d}{dt} (mc_P \theta)_{air} = mc_P \frac{d\theta}{dt} + \rho c_P \dot{V} \theta = \dot{Q} - hS\theta$$

Thermal Energy Dynamics
Sample heat Release rate
Heat losses by convection

$$\frac{d\theta}{dt} + \frac{\theta}{\tau} = \frac{\dot{Q}}{mc_P}$$

Governing Equation
HR2 Dynamics



Energy Balance Allows for Automatic (In Situ) Calibration

***HR2 Automatic
Calibration Factor***

$$k_{auto} \equiv \frac{\dot{Q}_{BL} + \dot{Q}_{sample}(t)}{\theta_{BL} + \Delta T_{sample}} = \frac{\dot{Q}_{BL} + \dot{Q}_{sample}(t)}{\theta(t)}$$

***Baseline
Combustion Rate***

$$\dot{Q}_{BL} = (\rho c_p \dot{V} + hS)_{air}$$

***Standard
Combustion Rate
(Methane Equivalent)***

$$\dot{Q}_{test} = \left\{ \frac{(\rho H_c \dot{V})_{CH_4}}{\Delta T_{CH_4}} \right\} \Delta T(t) = k_h \Delta T(t)$$

Static
Calibration
Factor

Heat Release Rate (Dynamic Calibration)

$$\begin{aligned}\text{HRR} \left(\frac{W}{m^2} \right) &= \frac{\dot{Q}(t)}{A} = \left\{ \frac{\dot{Q}_{BL}}{\theta} + \frac{\dot{Q}_{sample}}{\theta} \right\} \frac{\Delta T(t)}{A} \\ &= \left\{ \frac{(\rho c_P \dot{V} + hS)_{air} + k_h \Delta T(t)}{\theta(t)} \right\} \frac{\Delta T(t)}{A} \\ &= \left\{ \frac{c_1 + c_2 \Delta T(t)}{\theta(t)} \right\} \frac{\Delta T(t)}{A} \quad \begin{array}{l} \text{Constants} \\ \text{Measured} \end{array} \\ &\quad \longleftarrow k_{auto} \longrightarrow\end{aligned}$$

Baseline (BL) has all info needed for Dynamic Calibration

$$\theta_{BL} = T_{BL} - T_{in} = \frac{1}{k_{BL}} \left(\underset{(6000W)}{\dot{Q}_{glowbars}} + \underset{(900W)}{\dot{Q}_{pilot}} \right) = \frac{\dot{Q}_{BL}}{k_{BL}}$$

From static energy balances,

$$k_{BL} = \frac{\dot{Q}_{BL}}{\theta_{BL}} = \frac{6900W}{613K - 295K} = (\rho \dot{V} c_P + hS)_{air} = 20 \frac{W}{K} = k_h$$

Calibration constant is independent of energy source,

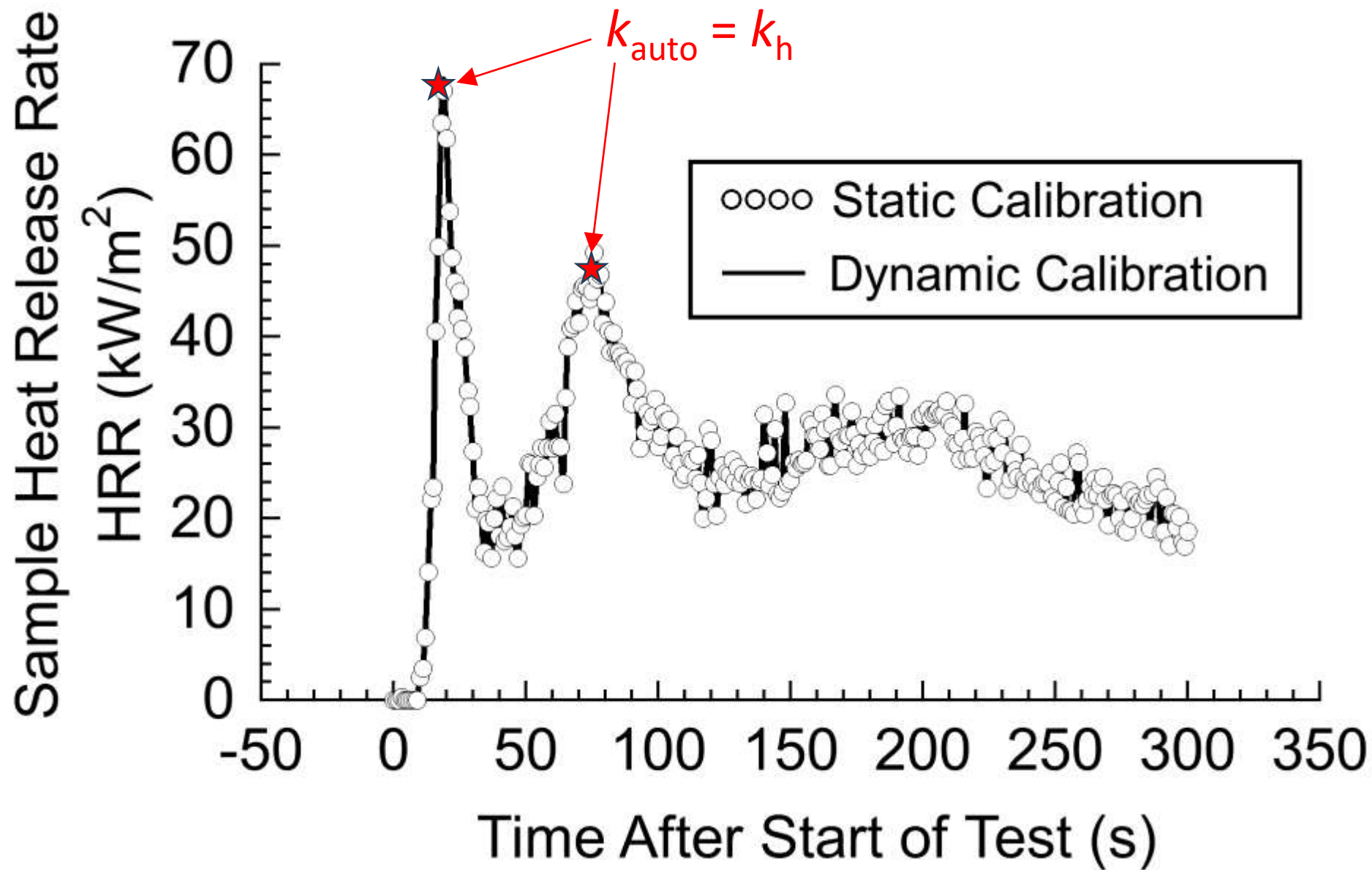
$$k_{auto} = \left(\frac{c_1 + c_2 \Delta T(t)}{\theta(t)} \right)_{c_2 = k_{BL}} = k_h$$

$k_{\text{auto}} = k_h$ only at Maximum Heat Release Rate (HRR_{max})

$$\frac{d}{dt} \left(\frac{d\theta}{dt} + \frac{\theta}{\tau} = \frac{\dot{Q}}{mc_P} \right) = \underbrace{\ddot{\theta}}_0 + \frac{\dot{\theta}}{\tau} = \underbrace{\frac{\ddot{Q}}{mc_P}}_0 = 0$$

$$\frac{\dot{\theta}}{\tau} = \frac{1}{\tau} \frac{d\theta}{dt} = \frac{1}{\tau} \frac{d\Delta T}{dt} = 0$$

$$\Delta T = \text{Constant} = \frac{\dot{Q}_{\text{max}}}{k_{\text{auto}}} = \frac{\dot{Q}_{\text{CH}_4}}{k_h} \Rightarrow \frac{\dot{Q}_{\text{max}}}{\dot{Q}_{\text{CH}_4}} = \frac{k_{\text{auto}}}{k_h} = 1 \quad \text{Only at } \dot{Q}_{\text{max}}$$



Conclusions

Position of heat sources (glowbars, pilots, sample) and sinks (sample fixture) in HR2 determine how much heat will be lost to apparatus and the value of k_{auto} and k_h used to measure HRR.

$$\text{HRR} \left(\frac{kW}{m^2} \right) = \underbrace{\left\{ \frac{(\rho c_P \dot{V} + hS)_{air} + k_h \Delta T(t)}{\theta(t)} \right\}}_{\text{Dynamic Calibration Factor}} \frac{\Delta T(t)}{A}$$

$$k_{auto} = \left\{ \frac{\textcolor{blue}{c_1} + \textcolor{blue}{c_2} \textcolor{red}{\Delta T(t)}}{\textcolor{red}{\theta(t)}} \right\} \quad \begin{array}{l} \textcolor{blue}{Constants} \\ \textcolor{red}{Measured} \end{array}$$

$$\textcolor{blue}{c_1} = (\rho c_P \dot{V} + hS)_{air} = \text{Heat transfer contribution to } k_{auto}$$